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Electrical Control System Modelling Formulas

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List of 16 Electrical Control System Modelling Formulas

Electrical Control System Modelling

Feedback Characteristics

1) Closed Loop Gain

$$\text{fx } A_c = \frac{1}{\beta}$$

[Open Calculator !\[\]\(de95854c7ee024cfadc48187bbb781b2_img.jpg\)](#)

$$\text{ex } 0.25 = \frac{1}{4}$$

2) Closed Loop Negative Feedback Gain

$$\text{fx } A_f = \frac{A_o}{1 + (\beta \cdot A_o)}$$

[Open Calculator !\[\]\(6a9b39b98eb945faa14c645ec99e4eaa_img.jpg\)](#)

$$\text{ex } 0.249984 = \frac{4000}{1 + (4 \cdot 4000)}$$

3) Closed Loop Positive Feedback Gain

$$\text{fx } A_f = \frac{A_o}{1 - (\beta \cdot A_o)}$$

[Open Calculator !\[\]\(f1c5da15572e3e09d343161be98f508d_img.jpg\)](#)

$$\text{ex } -0.250016 = \frac{4000}{1 - (4 \cdot 4000)}$$



4) Transfer Function for Closed and Open Loop System

$$\text{fx } G_s = \frac{C_s}{R_s}$$

[Open Calculator !\[\]\(cbe80b694ebd74fcfe136a095b608235_img.jpg\)](#)

$$\text{ex } 0.458333 = \frac{22}{48}$$

Modelling Parameters

5) Angle of Asymptotes

$$\text{fx } \phi_k = \frac{(2 \cdot (\text{modulus}(N - M) - 1) + 1) \cdot \pi}{\text{modulus}(N - M)}$$

[Open Calculator !\[\]\(5361750c22c4e047a52f4eac1ec2d4cc_img.jpg\)](#)

$$\text{ex } 5.834386\text{rad} = \frac{(2 \cdot (\text{modulus}(13 - 6) - 1) + 1) \cdot \pi}{\text{modulus}(13 - 6)}$$


6) Bandwidth Frequency given Damping Ratio

$$\text{fx } f_b = \omega_n \cdot \left(\sqrt{1 - (2 \cdot \zeta^2)} + \sqrt{\zeta^4 - (4 \cdot \zeta^2) + 2} \right)$$

[Open Calculator !\[\]\(b792654f2cef9719eabeb6c5be00811e_img.jpg\)](#)

$$\text{ex } 54.96966\text{Hz} = 23\text{Hz} \cdot \left(\sqrt{1 - (2 \cdot (0.1)^2)} + \sqrt{(0.1)^4 - (4 \cdot (0.1)^2) + 2} \right)$$




7) Damped Natural Frequency 

$$fx \quad \omega_d = \omega_n \cdot \sqrt{1 - \zeta^2}$$

Open Calculator 

$$ex \quad 22.88471\text{Hz} = 23\text{Hz} \cdot \sqrt{1 - (0.1)^2}$$

8) Damping Ratio given Critical Damping 

$$fx \quad \zeta = \frac{C}{C_c}$$

Open Calculator 

$$ex \quad 0.100334 = \frac{0.6}{5.98}$$


9) Damping Ratio given Percentage Overshoot 

$$fx \quad \zeta = - \frac{\ln\left(\frac{\%o}{100}\right)}{\sqrt{\pi^2 + \ln\left(\frac{\%o}{100}\right)^2}}$$

Open Calculator 

$$ex \quad 0.100106 = - \frac{\ln\left(\frac{72.9}{100}\right)}{\sqrt{\pi^2 + \ln\left(\frac{72.9}{100}\right)^2}}$$




10) Damping Ratio or Damping Factor 

$$fx \quad \zeta = \frac{c}{2 \cdot \sqrt{m \cdot K_{spring}}}$$

Open Calculator 


$$ex \quad 0.188147 = \frac{16}{2 \cdot \sqrt{35.45\text{kg} \cdot 51\text{N/m}}}$$

11) Gain-Bandwidth Product 

$$fx \quad G.B = \text{modulus}(A_M) \cdot BW$$

Open Calculator 

$$ex \quad 56.16\text{Hz} = \text{modulus}(0.78) \cdot 72\text{b/s}$$

12) Number of Asymptotes 

$$fx \quad N_a = N - M$$

Open Calculator 

$$ex \quad 7 = 13 - 6$$

13) Percentage Overshoot 

$$fx \quad \%o = 100 \cdot \left(e^{\frac{-\zeta \cdot \pi}{\sqrt{1-\zeta^2}}} \right)$$

Open Calculator 

$$ex \quad 72.92476 = 100 \cdot \left(e^{\frac{-0.1 \cdot \pi}{\sqrt{1-(0.1)^2}}} \right)$$



14) Q-Factor 

$$\text{fx } Q = \frac{1}{2 \cdot \zeta}$$

[Open Calculator](#) 


$$\text{ex } 5 = \frac{1}{2 \cdot 0.1}$$

15) Resonant Frequency 

$$\text{fx } \omega_r = \omega_n \cdot \sqrt{1 - 2 \cdot \zeta^2}$$

[Open Calculator](#) 

$$\text{ex } 22.76884\text{Hz} = 23\text{Hz} \cdot \sqrt{1 - 2 \cdot (0.1)^2}$$

16) Resonant Peak 

$$\text{fx } M_r = \frac{1}{2 \cdot \zeta \cdot \sqrt{1 - \zeta^2}}$$

[Open Calculator](#) 

$$\text{ex } 5.025189 = \frac{1}{2 \cdot 0.1 \cdot \sqrt{1 - (0.1)^2}}$$



Variables Used






- $\%O$ Percentage Overshoot
- A_C Closed-Loop Gain
- A_f Gain with Feedback
- A_M Amplifier Gain in Mid Band
- A_O Open Loop Gain of an OP-AMP
- **BW** Amplifier Bandwidth (*Bit Per Second*)
- c Damping Coefficient
- C Actual Damping
- C_C Critical Damping
- C_S Output of System
- f_b Bandwidth Frequency (*Hertz*)
- G_S Transfer Function
- **G.B** Gain-Bandwidth Product (*Hertz*)
- K_{Spring} Spring Constant (*Newton per Meter*)
- m Mass (*Kilogram*)
- M Number of Zeroes
- M_r Resonant Peak
- N Number of Poles
- N_a Number of Asymptotes
- Q Q Factor
- R_S Input of System
- β Feedback Factor



- ζ Damping Ratio
- ϕ_k Angle of Asymptotes (Radian)
- ω_d Damped Natural Frequency (Hertz)
- ω_n Natural Frequency of Oscillation (Hertz)
- ω_r Resonant Frequency (Hertz)



Constants, Functions, Measurements used

- **Constant:** π , 3.14159265358979323846264338327950288
Archimedes' constant
- **Constant:** e , 2.71828182845904523536028747135266249
Napier's constant
- **Function:** **ln**, $\ln(\text{Number})$
The natural logarithm, also known as the logarithm to the base e , is the inverse function of the natural exponential function.
- **Function:** **modulus**, modulus
Modulus of a number is the remainder when that number is divided by another number.
- **Function:** **sqrt**, $\sqrt{\text{Number}}$
A square root function is a function that takes a non-negative number as an input and returns the square root of the given input number.
- **Measurement:** **Weight** in Kilogram (kg)
Weight Unit Conversion 
- **Measurement:** **Angle** in Radian (rad)
Angle Unit Conversion 
- **Measurement:** **Frequency** in Hertz (Hz)
Frequency Unit Conversion 
- **Measurement:** **Bandwidth** in Bit Per Second (b/s)
Bandwidth Unit Conversion 
- **Measurement:** **Stiffness Constant** in Newton per Meter (N/m)
Stiffness Constant Unit Conversion 



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