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# Power System Stability Formulas

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# List of 20 Power System Stability Formulas

## Power System Stability

### 1) Accelerating Torque of Generator under Power System Stability

$$\text{fx } T_a = T_m - T_e$$

[Open Calculator !\[\]\(a870788d6ed9b8fd294b7654a8c8526b\_img.jpg\)](#)

$$\text{ex } 32\text{N}\cdot\text{m} = 44\text{N}\cdot\text{m} - 12\text{N}\cdot\text{m}$$

### 2) Active Power by Infinite Bus

$$\text{fx } P_{\text{inf}} = \frac{(V)^2}{\sqrt{(R)^2 + (X_s)^2}} - \frac{(V)^2}{(R)^2 + (X_s)^2}$$

[Open Calculator !\[\]\(c50c8b7b2cc2cf9ff925edec0ee94c0d\_img.jpg\)](#)

$$\text{ex } 2.084176\text{W} = \frac{(11\text{V})^2}{\sqrt{(2.1\Omega)^2 + (57\Omega)^2}} - \frac{(11\text{V})^2}{(2.1\Omega)^2 + (57\Omega)^2}$$

### 3) Angular Displacement of Machine under Power System Stability

$$\text{fx } \delta_a = \theta_m - \omega_s \cdot t$$

[Open Calculator !\[\]\(f60b7a900783ac3fd531bfd9c111be6d\_img.jpg\)](#)

$$\text{ex } 20.2\text{rad} = 109\text{rad} - 8\text{m/s} \cdot 11.1\text{s}$$



#### 4) Clearing Angle

$$\text{fx } \delta_c = \frac{\pi \cdot f \cdot P_i}{2 \cdot H} \cdot (t_c)^2 + \delta_o$$

[Open Calculator !\[\]\(cbe80b694ebd74fcfe136a095b608235\_img.jpg\)](#)

$$\text{ex } 61.93019\text{rad} = \frac{\pi \cdot 56\text{Hz} \cdot 200\text{W}}{2 \cdot 39\text{kg}\cdot\text{m}^2} \cdot (0.37\text{s})^2 + 10^\circ$$

#### 5) Clearing Time

$$\text{fx } t_c = \sqrt{\frac{2 \cdot H \cdot (\delta_c - \delta_o)}{\pi \cdot f \cdot P_i}}$$

[Open Calculator !\[\]\(3e2231b1ad3ca8da8658228c00dd08e0\_img.jpg\)](#)

$$\text{ex } 0.36991\text{s} = \sqrt{\frac{2 \cdot 39\text{kg}\cdot\text{m}^2 \cdot (61.9\text{rad} - 10^\circ)}{\pi \cdot 56\text{Hz} \cdot 200\text{W}}}$$

#### 6) Complex Power of Generator under Power Angle Curve

$$\text{fx } S = V_p \cdot I_p$$

[Open Calculator !\[\]\(0d5ec72f61334709c3fc9450209b754f\_img.jpg\)](#)

$$\text{ex } 1282.42\text{VA} = 74\text{V} \cdot 17.33\text{A}$$

#### 7) Critical Clearing Angle under Power System Stability

$$\text{fx } \delta_{cc} = a \cos \left( \cos(\delta_{\max}) + \left( \frac{P_i}{P_{\max}} \right) \cdot (\delta_{\max} - \delta_o) \right)$$

[Open Calculator !\[\]\(b64b40baaee5acddc1eab8538ba84754\_img.jpg\)](#)

$$\text{ex } 47.58211^\circ = a \cos \left( \cos(60^\circ) + \left( \frac{200\text{W}}{1000\text{W}} \right) \cdot (60^\circ - 10^\circ) \right)$$



## 8) Critical Clearing Time under Power System Stability

[Open Calculator !\[\]\(dfbd6b3763a6d1d9afaa974f64e2e4b5\_img.jpg\)](#)

$$\text{fx } t_{cc} = \sqrt{\frac{2 \cdot H \cdot (\delta_{cc} - \delta_o)}{\pi \cdot f \cdot P_{\max}}}$$

$$\text{ex } 0.017035s = \sqrt{\frac{2 \cdot 39\text{kg}\cdot\text{m}^2 \cdot (47.5^\circ - 10^\circ)}{\pi \cdot 56\text{Hz} \cdot 1000\text{W}}}$$

## 9) Damped Frequency of Oscillation in Power System Stability

[Open Calculator !\[\]\(ec9132f1d27c8919987d92907322654d\_img.jpg\)](#)

$$\text{fx } \omega_{df} = \omega_{fn} \cdot \sqrt{1 - (\xi)^2}$$

$$\text{ex } 8.954887\text{Hz} = 9\text{Hz} \cdot \sqrt{1 - (0.1)^2}$$

## 10) Inertia Constant of Machine

[Open Calculator !\[\]\(758ebdf4629c903da74c2e079717ae32\_img.jpg\)](#)

$$\text{fx } M = \frac{G \cdot H}{180 \cdot f_s}$$

$$\text{ex } 0.059091 = \frac{15 \cdot 39\text{kg}\cdot\text{m}^2}{180 \cdot 55\text{Hz}}$$

## 11) Kinetic Energy of Rotor

[Open Calculator !\[\]\(248b91fcdac4810ffd15cf33fb6aec6f\_img.jpg\)](#)

$$\text{fx } KE = \left(\frac{1}{2}\right) \cdot J \cdot \omega_s^2 \cdot 10^{-6}$$

$$\text{ex } 0.000192\text{J} = \left(\frac{1}{2}\right) \cdot 6.0\text{kg}\cdot\text{m}^2 \cdot (8\text{m/s})^2 \cdot 10^{-6}$$



## 12) Lossless Power Delivered in Synchronous Machine

$$\text{fx } P_1 = P_{\max} \cdot \sin(\delta)$$

[Open Calculator !\[\]\(e2376d476d06eb31946dc01a69a4403a\_img.jpg\)](#)

$$\text{ex } 707.1068\text{W} = 1000\text{W} \cdot \sin(45^\circ)$$

## 13) Maximum Steady State Power Transfer

$$\text{fx } P_{e,\max} = \frac{\text{modulus}(E_g) \cdot \text{modulus}(V)}{X_s}$$

[Open Calculator !\[\]\(0b5e7e25e8775f7e7e80906ada4f0021\_img.jpg\)](#)

$$\text{ex } 30.87719\text{V} = \frac{\text{modulus}(160\text{V}) \cdot \text{modulus}(11\text{V})}{57\Omega}$$

## 14) Moment of Inertia of Machine under Power System Stability

$$\text{fx } M_i = J \cdot \left(\frac{2}{P}\right)^2 \cdot \omega_r \cdot 10^{-6}$$

[Open Calculator !\[\]\(bd3b31712ad9bab5a241210fa6925cdd\_img.jpg\)](#)

$$\text{ex } 0.000726\text{kg}\cdot\text{m}^2 = 6.0\text{kg}\cdot\text{m}^2 \cdot \left(\frac{2}{2}\right)^2 \cdot 121\text{m/s} \cdot 10^{-6}$$

## 15) Output Power of Generator under Power System Stability

$$\text{fx } P_g = \frac{E_g \cdot V_t \cdot \sin(\zeta_{\text{op}})}{x_d}$$

[Open Calculator !\[\]\(7bc43b319a082987e20f7bf78f4bab80\_img.jpg\)](#)

$$\text{ex } 0.096\text{W} = \frac{160\text{V} \cdot 3\text{V} \cdot \sin(90^\circ)}{5000\text{AT/Wb}}$$



## 16) Real Power of Generator under Power Angle Curve

$$\text{fx } P_e = \frac{\text{modulus}(E_g) \cdot \text{modulus}(V)}{X_s} \cdot \sin(\delta)$$

[Open Calculator !\[\]\(d3fb9f94af8b26d1c844efa9a98805b0\_img.jpg\)](#)

$$\text{ex } 21.83347\text{W} = \frac{\text{modulus}(160\text{V}) \cdot \text{modulus}(11\text{V})}{57\Omega} \cdot \sin(45^\circ)$$

## 17) Rotor Acceleration

$$\text{fx } P_a = P_i - P_{ep}$$

[Open Calculator !\[\]\(e1d6102fe77919492c04879c8450f1f5\_img.jpg\)](#)

$$\text{ex } 100.1\text{W} = 200\text{W} - 99.9\text{W}$$

## 18) Speed of Synchronous Machine

$$\text{fx } \omega_{es} = \left( \frac{P}{2} \right) \cdot \omega_r$$

[Open Calculator !\[\]\(ab4e2b3fc7e7887b7a72f548aa6f5e60\_img.jpg\)](#)

$$\text{ex } 121\text{m/s} = \left( \frac{2}{2} \right) \cdot 121\text{m/s}$$

## 19) Synchronous Power of Power Angle Curve

$$\text{fx } P_{syn} = \frac{\text{modulus}(E_g) \cdot \text{modulus}(V)}{X_s} \cdot \cos(\delta)$$

[Open Calculator !\[\]\(5abce1a84a655b073239ab33e1199487\_img.jpg\)](#)

$$\text{ex } 21.83347\text{W} = \frac{\text{modulus}(160\text{V}) \cdot \text{modulus}(11\text{V})}{57\Omega} \cdot \cos(45^\circ)$$



## 20) Time Constant in Power System Stability

[Open Calculator !\[\]\(feabb98897b440bc8695a03336a6e2df\_img.jpg\)](#)

**fx** 
$$T = \frac{2 \cdot H}{\pi \cdot \omega_{df} \cdot D}$$

**ex** 
$$0.110964s = \frac{2 \cdot 39kg \cdot m^2}{\pi \cdot 8.95Hz \cdot 25Ns/m}$$



## Variables Used

- **D** Damping Coefficient (*Newton Second per Meter*)
- **E<sub>g</sub>** EMF of Generator (*Volt*)
- **f** Frequency (*Hertz*)
- **f<sub>s</sub>** Synchronous Frequency (*Hertz*)
- **G** Three Phase MVA Rating of Machine
- **H** Constant of Inertia (*Kilogram Square Meter*)
- **I<sub>p</sub>** Phasor Current (*Ampere*)
- **J** Rotor Moment of Inertia (*Kilogram Square Meter*)
- **KE** Kinetic Energy of Rotor (*Joule*)
- **M** Inertia Constant of Machine
- **M<sub>i</sub>** Moment of Inertia (*Kilogram Square Meter*)
- **P** Number of Machine Poles
- **P<sub>a</sub>** Accelerating Power (*Watt*)
- **P<sub>e</sub>** Real Power (*Watt*)
- **P<sub>e,max</sub>** Maximum Steady State Power Transfer (*Volt*)
- **P<sub>ep</sub>** Electromagnetic Power (*Watt*)
- **P<sub>g</sub>** Output Power of Generator (*Watt*)
- **P<sub>i</sub>** Input Power (*Watt*)
- **P<sub>inf</sub>** Active Power of Infinite Bus (*Watt*)
- **P<sub>l</sub>** Lossless Power Delivered (*Watt*)
- **P<sub>max</sub>** Maximum Power (*Watt*)
- **P<sub>syn</sub>** Synchronous Power (*Watt*)









- **R** Resistance (Ohm)
- **S** Complex Power (Volt Ampere)
- **t** Time of Angular Displacement (Second)
- **T** Time Constant (Second)
- **T<sub>a</sub>** Accelerating Torque (Newton Meter)
- **t<sub>c</sub>** Clearing Time (Second)
- **t<sub>cc</sub>** Critical Clearing Time (Second)
- **T<sub>e</sub>** Electrical Torque (Newton Meter)
- **T<sub>m</sub>** Mechanical Torque (Newton Meter)
- **V** Voltage of Infinite Bus (Volt)
- **V<sub>p</sub>** Phasor Voltage (Volt)
- **V<sub>t</sub>** Terminal Voltage (Volt)
- **x<sub>d</sub>** Magnetic Reluctance (Ampere-Turn per Weber)
- **X<sub>s</sub>** Synchronous Reactance (Ohm)
- **δ** Electrical Power Angle (Degree)
- **δ<sub>a</sub>** Angular Displacement of Machine (Radian)
- **δ<sub>c</sub>** Clearing Angle (Radian)
- **δ<sub>cc</sub>** Critical Clearing Angle (Degree)
- **δ<sub>max</sub>** Maximum Clearing Angle (Degree)
- **δ<sub>o</sub>** Initial Power Angle (Degree)
- **ζ<sub>op</sub>** Power Angle (Degree)
- **θ<sub>m</sub>** Angular Displacement of Rotor (Radian)
- **ξ** Oscillation Constant
- **ω<sub>df</sub>** Damping Frequency of Oscillation (Hertz)












- $\omega_{es}$  Speed of Synchronous Machine (Meter per Second)
- $\omega_{fn}$  Natural Frequency of Oscillation (Hertz)
- $\omega_r$  Rotor Speed of Synchronous Machine (Meter per Second)
- $\omega_s$  Synchronous Speed (Meter per Second)



# Constants, Functions, Measurements used




- **Constant:** **pi**, 3.14159265358979323846264338327950288  
*Archimedes' constant*
- **Function:** **acos**, `acos(Number)`  
*The inverse cosine function, is the inverse function of the cosine function. It is the function that takes a ratio as an input and returns the angle whose cosine is equal to that ratio.*
- **Function:** **cos**, `cos(Angle)`  
*Cosine of an angle is the ratio of the side adjacent to the angle to the hypotenuse of the triangle.*
- **Function:** **modulus**, `modulus`  
*Modulus of a number is the remainder when that number is divided by another number.*
- **Function:** **sin**, `sin(Angle)`  
*Sine is a trigonometric function that describes the ratio of the length of the opposite side of a right triangle to the length of the hypotenuse.*
- **Function:** **sqrt**, `sqrt(Number)`  
*A square root function is a function that takes a non-negative number as an input and returns the square root of the given input number.*
- **Measurement:** **Time** in Second (s)  
*Time Unit Conversion* 
- **Measurement:** **Electric Current** in Ampere (A)  
*Electric Current Unit Conversion* 
- **Measurement:** **Speed** in Meter per Second (m/s)  
*Speed Unit Conversion* 
- **Measurement:** **Energy** in Joule (J)  
*Energy Unit Conversion* 



- **Measurement: Power** in Watt (W), Volt Ampere (VA)  
*Power Unit Conversion* 
- **Measurement: Angle** in Radian (rad), Degree ( $^{\circ}$ )  
*Angle Unit Conversion* 
- **Measurement: Frequency** in Hertz (Hz)  
*Frequency Unit Conversion* 
- **Measurement: Electric Resistance** in Ohm ( $\Omega$ )  
*Electric Resistance Unit Conversion* 
- **Measurement: Electric Potential** in Volt (V)  
*Electric Potential Unit Conversion* 
- **Measurement: Torque** in Newton Meter (N\*m)  
*Torque Unit Conversion* 
- **Measurement: Moment of Inertia** in Kilogram Square Meter ( $\text{kg}\cdot\text{m}^2$ )  
*Moment of Inertia Unit Conversion* 
- **Measurement: Damping Coefficient** in Newton Second per Meter (Ns/m)  
*Damping Coefficient Unit Conversion* 
- **Measurement: Reluctance** in Ampere-Turn per Weber (AT/Wb)  
*Reluctance Unit Conversion* 



## Check other formula lists

- **Overhead AC Supply Formulas** 
- **Overhead DC Supply Formulas** 
- **Power System Stability Formulas** 
- **Underground AC Supply Formulas** 
- **Underground DC Supply Formulas** 

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