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Francis Turbine Formulas

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List of 18 Francis Turbine Formulas

Francis Turbine

1) Degree of Reaction of Turbine with Right Angled Outlet Blade

$$\text{fx } R = 1 - \frac{\cot(\alpha)}{2 \cdot (\cot(\alpha) - \cot(\theta))}$$

[Open Calculator !\[\]\(a870788d6ed9b8fd294b7654a8c8526b_img.jpg\)](#)

$$\text{ex } 0.450009 = 1 - \frac{\cot(11.03^\circ)}{2 \cdot (\cot(11.03^\circ) - \cot(65^\circ))}$$

2) Francis Turbine Flow Ratio

$$\text{fx } K_f = \frac{V_{f1}}{\sqrt{2 \cdot g \cdot H_i}}$$

[Open Calculator !\[\]\(c50c8b7b2cc2cf9ff925edec0ee94c0d_img.jpg\)](#)

$$\text{ex } 0.160326 = \frac{2.3\text{m/s}}{\sqrt{2 \cdot 9.8\text{m/s}^2 \cdot 10.5\text{m}}}$$

3) Francis Turbine Speed Ratio

$$\text{fx } K_u = \frac{u_1}{\sqrt{2 \cdot g \cdot H_i}}$$

[Open Calculator !\[\]\(f60b7a900783ac3fd531bfd9c111be6d_img.jpg\)](#)

$$\text{ex } 0.658733 = \frac{9.45\text{m/s}}{\sqrt{2 \cdot 9.8\text{m/s}^2 \cdot 10.5\text{m}}}$$



4) Guide Blade Angle given Degree of Reaction 

$$\text{fx } \alpha = a \cot \left(\frac{\cot(\theta)}{1 - \frac{1}{2 \cdot (1-R)}} \right)$$

Open Calculator 


$$\text{ex } 11.03173^\circ = a \cot \left(\frac{\cot(65^\circ)}{1 - \frac{1}{2 \cdot (1-0.45)}} \right)$$

5) Pressure Head given Flow Ratio in Francis Turbine 

$$\text{fx } H_i = \frac{\left(\frac{V_{f1}}{K_f} \right)^2}{2 \cdot g}$$

Open Calculator 

$$\text{ex } 10.54289\text{m} = \frac{\left(\frac{2.3\text{m/s}}{0.16} \right)^2}{2 \cdot 9.8\text{m/s}^2}$$

6) Pressure Head given Speed Ratio in Francis Turbine 

$$\text{fx } H_i = \frac{\left(\frac{u_1}{K_u} \right)^2}{2 \cdot g}$$

Open Calculator 

$$\text{ex } 10.52339\text{m} = \frac{\left(\frac{9.45\text{m/s}}{0.658} \right)^2}{2 \cdot 9.8\text{m/s}^2}$$



7) Vane Angle at Inlet from Degree of Reaction 

$$\text{fx } \theta = a \cot \left(\cot(\alpha) \cdot \left(1 - \frac{1}{2 \cdot (1 - R)} \right) \right)$$

Open Calculator 


$$\text{ex } 64.99646^\circ = a \cot \left(\cot(11.03^\circ) \cdot \left(1 - \frac{1}{2 \cdot (1 - 0.45)} \right) \right)$$

8) Velocity of Flow at Inlet given Flow Ratio in Francis Turbine 

$$\text{fx } V_{f1} = K_f \cdot \sqrt{2 \cdot g \cdot H_i}$$

Open Calculator 


$$\text{ex } 2.295317\text{m/s} = 0.16 \cdot \sqrt{2 \cdot 9.8\text{m/s}^2 \cdot 10.5\text{m}}$$

9) Velocity of Vane at Inlet given Speed Ratio Francis Turbine 

$$\text{fx } u_1 = K_u \cdot \sqrt{2 \cdot g \cdot H_i}$$

Open Calculator 

$$\text{ex } 9.439491\text{m/s} = 0.658 \cdot \sqrt{2 \cdot 9.8\text{m/s}^2 \cdot 10.5\text{m}}$$

Hydraulic Efficiency 10) Hydraulic Efficiency of Francis Turbine with Acute Angled Outlet Blade 

$$\text{fx } \eta_h = \frac{V_{w1} \cdot u_1 + V_{w2} \cdot u_2}{g \cdot H}$$

Open Calculator 

$$\text{ex } 0.726813 = \frac{12.93\text{m/s} \cdot 9.45\text{m/s} + 6.5\text{m/s} \cdot 5.2\text{m/s}}{9.8\text{m/s}^2 \cdot 21.9\text{m}}$$



11) Hydraulic Efficiency of Francis Turbine with Obtuse Angled Outlet Blade

$$\text{fx } \eta_h = \frac{V_{w1} \cdot u_1 - V_{w2} \cdot u_2}{g \cdot H}$$

[Open Calculator !\[\]\(e2376d476d06eb31946dc01a69a4403a_img.jpg\)](#)

$$\text{ex } 0.411837 = \frac{12.93\text{m/s} \cdot 9.45\text{m/s} - 6.5\text{m/s} \cdot 5.2\text{m/s}}{9.8\text{m/s}^2 \cdot 21.9\text{m}}$$

12) Hydraulic Efficiency of Francis Turbine with Right Angled Outlet Blade

$$\text{fx } \eta_h = \frac{V_{w1} \cdot u_1}{g \cdot H}$$

[Open Calculator !\[\]\(0b5e7e25e8775f7e7e80906ada4f0021_img.jpg\)](#)

$$\text{ex } 0.569325 = \frac{12.93\text{m/s} \cdot 9.45\text{m/s}}{9.8\text{m/s}^2 \cdot 21.9\text{m}}$$

Power Developed

13) Work Done per sec on Runner by Water for Obtuse Angled Outlet Blade

$$\text{fx } W = \rho \cdot Q \cdot (V_{w1} \cdot u_1 - V_{w2} \cdot u_2)$$

[Open Calculator !\[\]\(0fb13ad0bfa3d86868cdd3883e5665b3_img.jpg\)](#)

$$\text{ex } 132.5828\text{kW} = 1000\text{kg/m}^3 \cdot 1.5\text{m}^3/\text{s} \cdot (12.93\text{m/s} \cdot 9.45\text{m/s} - 6.5\text{m/s} \cdot 5.2\text{m/s})$$

14) Work Done per Second on Runner by Water for Acute Angled Outlet Blade

$$\text{fx } W = \rho \cdot Q \cdot (V_{w1} \cdot u_1 + V_{w2} \cdot u_2)$$

[Open Calculator !\[\]\(e50091943b385fe16d3277389202856f_img.jpg\)](#)

$$\text{ex } 233.9828\text{kW} = 1000\text{kg/m}^3 \cdot 1.5\text{m}^3/\text{s} \cdot (12.93\text{m/s} \cdot 9.45\text{m/s} + 6.5\text{m/s} \cdot 5.2\text{m/s})$$



15) Work Done per Second on Runner by Water for Right Angled Outlet Blade Angle

$$\text{fx } W = \rho \cdot Q \cdot u_1 \cdot V_{w1}$$

[Open Calculator !\[\]\(d3fb9f94af8b26d1c844efa9a98805b0_img.jpg\)](#)

$$\text{ex } 183.2827\text{kW} = 1000\text{kg/m}^3 \cdot 1.5\text{m}^3/\text{s} \cdot 9.45\text{m/s} \cdot 12.93\text{m/s}$$

Volume Flow Rate

16) Volume Flow Rate of Acute Angled Francis Turbine given Work Done Per Second on Runner

$$\text{fx } Q = \frac{W}{\rho \cdot (V_{w1} \cdot u_1 + V_{w2} \cdot u_2)}$$

[Open Calculator !\[\]\(73002692dd5e7a64e60946be3158e719_img.jpg\)](#)

$$\text{ex } 1.173163\text{m}^3/\text{s} = \frac{183\text{kW}}{1000\text{kg/m}^3 \cdot (12.93\text{m/s} \cdot 9.45\text{m/s} + 6.5\text{m/s} \cdot 5.2\text{m/s})}$$

17) Volume Flow Rate of Obtuse Angled Outlet Bladed Francis Turbine given Work Done per Second

$$\text{fx } Q = \frac{W}{\rho \cdot (V_{w1} \cdot u_1 - V_{w2} \cdot u_2)}$$

[Open Calculator !\[\]\(104fbf564e2e5a8fbd84f31656d114c7_img.jpg\)](#)

$$\text{ex } 2.070405\text{m}^3/\text{s} = \frac{183\text{kW}}{1000\text{kg/m}^3 \cdot (12.93\text{m/s} \cdot 9.45\text{m/s} - 6.5\text{m/s} \cdot 5.2\text{m/s})}$$



18) Volume Flow Rate of Right Angled Outlet Bladed Francis Turbine given Work Done per Second

fx

$$Q = \frac{W}{\rho \cdot u_1 \cdot V_{w1}}$$

[Open Calculator !\[\]\(83f22ed94ec5517769dd76d702c6bfd8_img.jpg\)](#)**ex**

$$1.497686\text{m}^3/\text{s} = \frac{183\text{kW}}{1000\text{kg}/\text{m}^3 \cdot 9.45\text{m}/\text{s} \cdot 12.93\text{m}/\text{s}}$$










Variables Used

- **g** Acceleration due to Gravity (*Meter per Square Second*)
- **H** Net Francis Turbine Head (*Meter*)
- **H_i** Head at Inlet of Francis Turbine (*Meter*)
- **K_f** Flow Ratio of Francis Turbine
- **K_u** Speed Ratio of Francis Turbine
- **Q** Volume Flow Rate for Francis Turbine (*Cubic Meter per Second*)
- **R** Degree of Reaction
- **u₁** Velocity of Vane at Inlet for Francis Turbine (*Meter per Second*)
- **u₂** Velocity of Vane at Outlet for Francis Turbine (*Meter per Second*)
- **V_{f1}** Velocity of Flow at Inlet of Francis Turbine (*Meter per Second*)
- **V_{w1}** Whirl Velocity at Inlet of Francis Turbine (*Meter per Second*)
- **V_{w2}** Whirl Velocity at Outlet of Francis Turbine (*Meter per Second*)
- **W** Work Done per Second by Francis Turbine (*Kilowatt*)
- **α** Guide Blade Angle (*Degree*)
- **η_h** Hydraulic Efficiency of Francis Turbine
- **θ** Vane Angle at Inlet (*Degree*)
- **ρ** Density of Fluid in Francis Turbine (*Kilogram per Cubic Meter*)




Constants, Functions, Measurements used

- **Function: acot**, acot(Number)
Inverse trigonometric cotangent function
- **Function: cot**, cot(Angle)
Trigonometric cotangent function
- **Function: sqrt**, sqrt(Number)
Square root function
- **Measurement: Length** in Meter (m)
Length Unit Conversion 
- **Measurement: Speed** in Meter per Second (m/s)
Speed Unit Conversion 
- **Measurement: Acceleration** in Meter per Square Second (m/s²)
Acceleration Unit Conversion 
- **Measurement: Power** in Kilowatt (kW)
Power Unit Conversion 
- **Measurement: Angle** in Degree (°)
Angle Unit Conversion 
- **Measurement: Volumetric Flow Rate** in Cubic Meter per Second (m³/s)
Volumetric Flow Rate Unit Conversion 
- **Measurement: Density** in Kilogram per Cubic Meter (kg/m³)
Density Unit Conversion 



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