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Frequency of Under Damped Forced Vibrations Formulas

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List of 15 Frequency of Under Damped Forced Vibrations Formulas

Frequency of Under Damped Forced Vibrations

1) Complementary Function

$$fx \quad x_1 = A \cdot \cos(\omega_d - \phi)$$

[Open Calculator !\[\]\(a870788d6ed9b8fd294b7654a8c8526b_img.jpg\)](#)

$$ex \quad 1.689698m = 5.25m \cdot \cos(6Hz - 55^\circ)$$

2) Damping Coefficient

$$fx \quad c = \frac{\tan(\phi) \cdot (k - m \cdot \omega^2)}{\omega}$$

[Open Calculator !\[\]\(c50c8b7b2cc2cf9ff925edec0ee94c0d_img.jpg\)](#)

$$ex \quad 4.998518Ns/m = \frac{\tan(55^\circ) \cdot (60N/m - .25kg \cdot (10rad/s)^2)}{10rad/s}$$

3) Deflection of System under Static Force

$$fx \quad x_o = \frac{F_x}{k}$$

[Open Calculator !\[\]\(f60b7a900783ac3fd531bfd9c111be6d_img.jpg\)](#)

$$ex \quad 0.333333m = \frac{20N}{60N/m}$$

4) External Periodic Disturbing Force

$$fx \quad F = F_x \cdot \cos(\omega \cdot t_p)$$

[Open Calculator !\[\]\(83bbbd261710c59db0214aa27b2edc0d_img.jpg\)](#)

$$ex \quad 16.87708N = 20N \cdot \cos(10rad/s \cdot 1.2s)$$



5) Maximum Displacement of Forced Vibration [Open Calculator !\[\]\(4729e517bc6a7cd81c8025b9646574fb_img.jpg\)](#)

$$fx \quad d_{\max} = \frac{F_x}{\sqrt{(c \cdot \omega)^2 - (k - m \cdot \omega^2)^2}}$$

$$ex \quad 0.560112m = \frac{20N}{\sqrt{(5Ns/m \cdot 10rad/s)^2 - (60N/m - .25kg \cdot (10rad/s)^2)^2}}$$

6) Maximum Displacement of Forced Vibration at Resonance [Open Calculator !\[\]\(e474458956c9a37fbf9586ddb60a7fa1_img.jpg\)](#)

$$fx \quad d_{\max} = x_o \cdot \frac{k}{c \cdot \omega_n}$$

$$ex \quad 0.56101m = 0.3333333m \cdot \frac{60N/m}{5Ns/m \cdot 7.13rad/s}$$

7) Maximum Displacement of Forced Vibration using Natural Frequency [Open Calculator !\[\]\(4fe57c3593bf1b21d272ae7ac8dfaf77_img.jpg\)](#)

$$fx \quad d_{\max} = \frac{x_o}{\sqrt{\frac{(c^2) \cdot (\omega^2)}{k^2} + \left(1 - \left(\frac{\omega^2}{\omega_n^2}\right)\right)^2}}$$

$$ex \quad 0.188476m = \frac{0.3333333m}{\sqrt{\frac{(5Ns/m)^2 \cdot (10rad/s)^2}{(60N/m)^2} + \left(1 - \left(\frac{(10rad/s)^2}{(7.13rad/s)^2}\right)\right)^2}}$$

8) Maximum Displacement of Forced Vibration with Negligible Damping [Open Calculator !\[\]\(2bae76de5ebbd5c4d7d47162f1673734_img.jpg\)](#)

$$fx \quad d_{\max} = \frac{F_x}{m \cdot (\omega_n^2 - \omega^2)}$$

$$ex \quad -1.627237m = \frac{20N}{.25kg \cdot ((7.13rad/s)^2 - (10rad/s)^2)}$$



9) Particular Integral 

$$fx \quad x_2 = \frac{F_x \cdot \cos(\omega \cdot t_p - \phi)}{\sqrt{(c \cdot \omega)^2 - (k - m \cdot \omega^2)^2}}$$

Open Calculator 

$$ex \quad 0.024914m = \frac{20N \cdot \cos(10rad/s \cdot 1.2s - 55^\circ)}{\sqrt{(5Ns/m \cdot 10rad/s)^2 - (60N/m - .25kg \cdot (10rad/s)^2)^2}}$$

10) Phase Constant 

$$fx \quad \phi = a \tan\left(\frac{c \cdot \omega}{k - m \cdot \omega^2}\right)$$

Open Calculator 

$$ex \quad 55.00798^\circ = a \tan\left(\frac{5Ns/m \cdot 10rad/s}{60N/m - .25kg \cdot (10rad/s)^2}\right)$$

11) Static Force 

$$fx \quad F_x = x_o \cdot k$$

Open Calculator 

$$ex \quad 20N = 0.3333333m \cdot 60N/m$$

12) Static Force using Maximum Displacement or Amplitude of Forced Vibration 

$$fx \quad F_x = d_{max} \cdot \left(\sqrt{(c \cdot \omega)^2 - (k - m \cdot \omega^2)^2}\right)$$

Open Calculator 

$$ex \quad 20.03171N = 0.561m \cdot \left(\sqrt{(5Ns/m \cdot 10rad/s)^2 - (60N/m - .25kg \cdot (10rad/s)^2)^2}\right)$$

13) Static Force when Damping is Negligible 

$$fx \quad F_x = d_{max} \cdot (m \cdot \omega_n^2 - \omega^2)$$

Open Calculator 

$$ex \quad -48.970125N = 0.561m \cdot (.25kg \cdot (7.13rad/s)^2 - (10rad/s)^2)$$



14) Total Displacement of Forced Vibration given Particular Integral and Complementary Function 

$$f_x \quad d_{tot} = x_2 + x_1$$

[Open Calculator !\[\]\(e2376d476d06eb31946dc01a69a4403a_img.jpg\)](#)

$$ex \quad 1.7m = 0.02m + 1.68m$$

15) Total Displacement of Forced Vibrations 

$$f_x \quad d_{tot} = A \cdot \cos(\omega_d - \phi) + \frac{F_x \cdot \cos(\omega \cdot t_p - \phi)}{\sqrt{(c \cdot \omega)^2 - (k - m \cdot \omega^2)^2}}$$

[Open Calculator !\[\]\(0b5e7e25e8775f7e7e80906ada4f0021_img.jpg\)](#)

$$ex \quad 1.714612m = 5.25m \cdot \cos(6Hz - 55^\circ) + \frac{20N \cdot \cos(10rad/s \cdot 1.2s - 55^\circ)}{\sqrt{(5Ns/m \cdot 10rad/s)^2 - (60N/m - .25kg \cdot (10rad/s)^2)^2}}$$



Variables Used

- **A** Amplitude of Vibration (Meter)
- **c** Damping Coefficient (Newton Second per Meter)
- **d_{max}** Maximum Displacement (Meter)
- **d_{tot}** Total Displacement (Meter)
- **F** External Periodic Disturbing Force (Newton)
- **F_x** Static Force (Newton)
- **k** Stiffness of Spring (Newton per Meter)
- **m** Mass suspended from Spring (Kilogram)
- **t_p** Time Period (Second)
- **x₁** Complementary Function (Meter)
- **x₂** Particular Integral (Meter)
- **x_o** Deflection under Static Force (Meter)
- **ϕ** Phase Constant (Degree)
- **ω** Angular Velocity (Radian per Second)
- **ω_d** Circular Damped Frequency (Hertz)
- **ω_n** Natural Circular Frequency (Radian per Second)



Constants, Functions, Measurements used

- **Function: atan**, atan(Number)
Inverse tan is used to calculate the angle by applying the tangent ratio of the angle, which is the opposite side divided by the adjacent side of the right triangle.
- **Function: cos**, cos(Angle)
Cosine of an angle is the ratio of the side adjacent to the angle to the hypotenuse of the triangle.
- **Function: sqrt**, sqrt(Number)
A square root function is a function that takes a non-negative number as an input and returns the square root of the given input number.
- **Function: tan**, tan(Angle)
The tangent of an angle is a trigonometric ratio of the length of the side opposite an angle to the length of the side adjacent to an angle in a right triangle.
- **Measurement: Length** in Meter (m)
Length Unit Conversion 
- **Measurement: Weight** in Kilogram (kg)
Weight Unit Conversion 
- **Measurement: Time** in Second (s)
Time Unit Conversion 
- **Measurement: Force** in Newton (N)
Force Unit Conversion 
- **Measurement: Angle** in Degree (°)
Angle Unit Conversion 
- **Measurement: Frequency** in Hertz (Hz)
Frequency Unit Conversion 
- **Measurement: Surface Tension** in Newton per Meter (N/m)
Surface Tension Unit Conversion 
- **Measurement: Angular Velocity** in Radian per Second (rad/s)
Angular Velocity Unit Conversion 
- **Measurement: Damping Coefficient** in Newton Second per Meter (Ns/m)
Damping Coefficient Unit Conversion 



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